

Technical Report: NAVTRAEQUIPCEN IH-200

ANALYSIS OF UNDERWATER ACOUSTIC
PROGATION LOSS MATH MODELS IN
CURRENT TRAINING DEVICES

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August 1972

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NAVAL TRAINING EQUIPMENT CENTER
ORLANDO, FLORIDA 32813

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ABSTRACT

This report analyzes and compares the various simulation designs and math models of underwater acoustic simulation presently being utilized in current training devices developed by the Naval Training Device Center. The analysis contains model simplifications and their affects on acoustic propagation loss. The comparative analysis includes Device 14E19, Basic AN/SQS-26 Sonar Operator Trainer; Device 14B44, P-3C DIFAR Operator Trainer; Device 2F69, P-3A Weapon System Trainer; Device 21A37, Submarine Fleet Ballistic Missile Training Facility; and Device 21A39/2, Sonar Room Tactical Team Trainer. The results of these models are then compared with the results of the ray trace model developed by the Naval Air Development Center.

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Advanced Systems Engineering Department

August 1972

Approved:

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SECTION I

ANALYSIS OF UNDERWATER ACOUSTIC PROPAGATION LOSS MATH MODELS IN CURRENT TRAINING DEVICES

INTRODUCTION

This report analyzes and compares the various simulation designs and math models of underwater acoustic simulation presently being utilized in current training devices developed by the NAVTRADEVCEN.

First, the basic underwater acoustic terms are defined which are required in the discussion of the various math models. Secondly, a study and comparative analysis is made of the propagation loss models utilized in five current training devices.

I.I SOUND PROPAGATION LOSSES IN THE OCEAN

As sound travels through the ocean, the pressure associated with the wave front diminishes, this decrease in pressure is referred to as propagation loss. There are three factors which contribute to this loss.

a. Spreading Loss. Spreading of the wave front causes the total energy associated with the wave front to be distributed over a larger area, resulting in a decrease in intensity. This loss is generated by the inverse square spreading law. As the energy travels away from the source, it spreads in the form of spherical shell. The decrease in intensity is exactly proportional to the increase in the surface area of the sphere. Since the surface area is given by $A=4\pi R^2$ the decrease in intensity is proportional to the square of the radius. The loss in dB due to spreading between a point one yard from the source and the receiver is given by:

Spherical Spreading Loss (db) = $10 \log R^2 = 20 \log R$

where R is the range in yards between the source and receiver. The intensity loss from spherical spreading increases about 6 dB per distance doubled.

In cylindrical spreading, the wave front expands in the form of a cylinder having a constant height which is determined by the thickness of the sound channel or sound duct. Cylindrical spreading loss is one-half of the spherical spreading loss in dB over equal ranges, and is presented by 10 log R in place of 20 log R. Therefore, intensity loss from cylindrical spreading increases about 3 dB per distance doubled and is given by:

Cylindrical Spreading Loss (dB) = 10 log R.

b. Attenuation Loss. The reduction in sound pressure level due to absorption and scattering is usually termed attenuation loss. Absorption is essentially the conversion of acoustic energy to heat. As a sound wave passes through the ocean it is accompanied by successive compressions and expansions of the medium which produces some frictional heat loss from the sound wave as well as heat loss produced by the disassociation of dissolved salts in sea water.

Although scattering is a component in the attenuation of sound, its contribution is not as important as that of absorption. When sound rays strike reflectors such as bubbles, fish, and suspended matter, sound energy is reflected away from the direction in which the major portion of the sound field is traveling, so that the wave itself suffers a loss in energy and hence, the intensity decreases.

c. Reflection. The surface of the ocean is rarely smooth; therefore, sound energy striking it is seldom reflected specularly (mirror reflection). Since the ocean surface is constantly changing, the sound energy is reflected in many directions. Surface reflection is a function of both sea state and frequency.

The ocean bottom may also reflect sound waves. Sound reflected from the ocean bottom usually suffers a significant loss in intensity. Part of this loss is due to scattering effects discussed above. The ocean bottom may be irregular and consequently reflect sound in many directions. The amount of energy lost through scattering will vary with the roughness of the bottom and frequency. Most of the bottom loss, however, results from the fact that a portion of the sound energy will enter the bottom and travel in it as a new sound wave. The amount of energy which is lost into the bottom will vary with the composition of the bottom, frequency of the sound wave, and the angle at which the sound wave strikes the bottom.

The total propagation loss over any given path is the sum of the losses due to spreading, attenuation, and reflection. Each of these component losses is subject to some degree of variability and uncerttainty. For these reasons the total propagation loss of sound waves traveling between any two points in the ocean cannot be predicted exactly. In practice, the propagation loss over any particular path can only be estimated by use of average measured values obtained from many observations.

1.2 DEVICE 14E19 PROPAGATION LOSS MODELS

This section provides the propagation loss models for Basic AN/SQS-26 Sonar Operator Trainer, Device 14E19 (reference 1). The propagation loss models used to simulate AN/SQS-26 surface duct mode of propagation are based upon the AMOS (Acoustic Meterological, and Oceanographic Survey) equations (references 2 and 3). AMOS variables and definitions are as follows:

L = Surface isothermal layer depth (ft)

S = Sea state

T = Water temperature (°F)

R = Range (kyds)

 $Z_0 = 0$ wn ship depth (ft)

z = Target depth (ft)

f = Acoustic freq. (kHz)

 $N_w = Transmission loss (db)$

a = Absorption coeff. (db/kyd)

 a_s = Scattering coeff (db/kyd)

G = First depth loss factor (db)

H = Second depth loss factor (db)

The basic AMOS propagation loss equations are divided into three primary zones. Analytical definitions of these zones and corresponding propagation loss equations are as follows:

a. Direct Radiation Zone $(0 \le r \le 1)$

When both ends of the transmission path lie within or at the bottom of the surface layer, $0 \le z_0 \le 1$, $0 \le z \le 1$, the following equation applies:

$$Nw = 20 \log R + aR + G (z-z_0) r + 60.$$
 (3.1)

At all other times the smaller of the two transmission losses computed using equation (3.1) and equation (3.2) is used.

$$Nw_2 = 20 \log R + aR + [25 - \sqrt{Z - L}] - \sqrt{Z_0 - L}] + 25] (f/25) + 60$$
 (3.2)

The term within the brackets is taken to be zero where it is negative.

b. Zone of First Order Surface Reflection ($z_0 \le 1$, $r_1 \le r \le r_1 + 1/2$)

Energy has been reflected at least once from the surface, the following is used:

$$Nw_3 = 20 \log R + aR + 2 (r-r_1) H (z, z_0) + [1-2 (r-r_1)] G (z-z_0) + 60 (3.3)$$

The shadow zone beyond the limiting ray is delineated by:

$$z_0 \le 1$$
, $z \le 1$, $r_1 \le r \le (r_1 + 1/2)$

For this zone equation (3.3) or equation (3.2) is used, whichever is smaller.

c. Zone of the Second or Higher Order Surface Reflection

$$(z_0 \le 1, r_1 + \frac{1}{2} \le r)$$

The following equation is used:

$$Nw_4 = 10 \log R + (a + a_s) R + H (z, z_0) - a \sqrt{L} (r_1 + \frac{1}{2}) + 10 \log [\sqrt{L} (r_1 + \frac{1}{2})] + 60$$
 (3.4)

The shadow zone beyond the limiting ray is delineated by:

$$z_0 \ge 1$$
, $z \ge 1$, $r_1 + \frac{1}{2} \le r$

For this zone, equation (3.4) or (3.2) is used, whichever yields the smaller propagation loss.

The required parameters are as follows:

(1) Scaled Variables

$$r = \frac{R}{\sqrt{L}}$$

$$z = \sqrt{\frac{Z_0}{L}}$$

$$z_0 = \sqrt{\frac{Z_0}{L}}$$

$$r_1 = \frac{1}{4}[2 - z - z_0]$$

$$z < 1, z_0 < 1$$

$$r_1 = \frac{1}{4}[z_0 - z - z_0]$$

$$z > 1, z_0 \ge 1$$

(2) Absorption Coefficient (db/kyd)

$$a = \frac{Af^{2} f_{T}}{f^{2} + f_{T}^{2}} + \frac{Bf^{2}}{f_{T}}$$

where A = .651 B = .0269 and f = $1.23 \times 10^6 \times e^{-4830/(T + 459.6)}$

For frequencies less than 4 kHz

$$a = \frac{.678 \text{ f}^2}{f_T}$$

(3) Scattering Attenuation Coefficient (db/kyd)

$$a_s = 4.5 \sqrt{\frac{f}{L}}$$

$$a_S = 9 \sqrt{\frac{f}{L}}$$
 $s \ge 3$

(4) First Depth Loss Factor (db) G as a function of $z-z_0$ is defined as follows:

G
$$(z - z_0) = .1 \times 10^{2 \cdot 3} (z - z_0) (f/25)^{1/3}$$

G $(z - z_0) = 20 (f/25)$
 $z - z_0 < 1$
 $z - z_0 \ge 1$

(5) Second Depth Loss Factor (db) H as a function of z_1 , and z_0 is defined as follows:

$$H(z_1,z_0) = F(z-z_0) + F(z) + F(z_0)$$

where x is a dummy variable and F (x) is defined as follows:

$$F(x) = .4 \times 10^{X} (f/8)^{1/3}$$
 $F > 8 \text{ kHz}$
 $F(x) = .4 \times 10^{X}$ $F < 8 \text{ kHz}$

The objective of this subsection is to present the analytic functions that are used to simulate the AN/SQS-26 bottom bounce mode of propagation. Bottom bounce conditions will be assumed to exist only for bottom depths of 6,400 feet or greater and deflection/elevation angles greater than or equal to 10 degrees. For all other conditions, it is assumed that propagation takes place via surface duct or shallow water conditions. These assumptions are based upon the recommended modes of operation given in reference 4. For the simulation, it is assumed that the propagation loss to the target from the point of transmission is equal to the loss from the sound source to the point of reception. Based on this assumption, the one-way path loss in db for the bottom path is:

$$Nw_B = 20 \log R_S + aR_S + L_B (\theta_{TB})$$

where $R_s = Slant range (yds)$

a = Attentuation coeff (db/yd)

 $L_B = Bottom Loss (db)$

 θ TB = Real bottom grazing angle (degrees)

Initially a function is required that determines the vertical angle $^\theta Bi$ as follows: $^\theta Bi$ = tan^{-1} $\frac{2^0Bi$ - 0T

where $D_{Bi} = Depth of bottom$

DT = Depth of target

RH = Horizontal range

These variables are shown in figure 1.

Total slant range is calculated by the following equation:

$$R_{s} = \frac{D_{Bi}}{\sin \theta_{Bi}} + \frac{D_{Bi} - D_{T}}{\sin \theta_{Bi}} = \frac{2D_{Bi} - D_{T}}{\sin \theta_{Bi}}$$

The isovelocity angle $\theta_{\mbox{\footnotesize{Bj}}}$ is converted to a real angle equivalent in order to provide the real transmitted beam deviation loss angles to the target. The transmitted deviation loss angle is calculated as follows:

$$\theta_{\text{Tbi}} = -a_1 + \frac{\sqrt{a_1^2 - 4a_2 (a_0 - \theta_{\text{Bi}})}}{2a_2}$$

The a coefficients were generated by Honeywell and are included in table 1. θ_{TB} is the real bottom grazing angle and is given by the following equation:

$$\cos \theta_{TB} = c^1 \cos \theta_{TBi}$$

where c^{1} are constants generated by Honeywell and given in table 2.

The attenuation coefficient is given by:

$$a = .033 (f)^{3/2}$$

where f = frequency (kHz)

and bottom loss simulation functions are analytically described by the following:

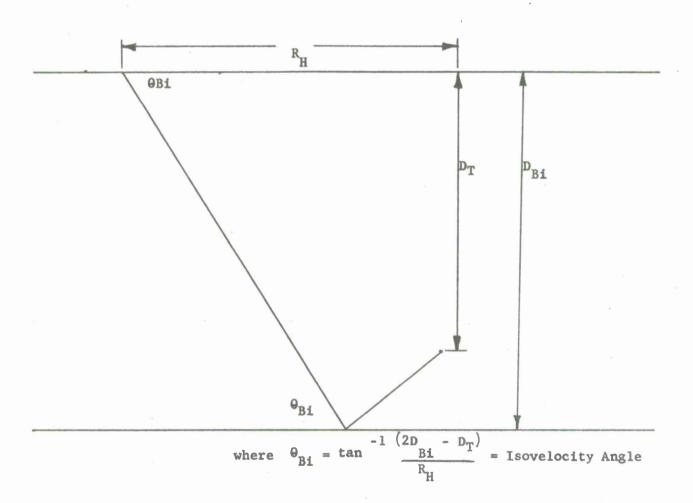


Figure 1. Ray Angles Defined

TABLE 1. ISOVELOCITY/REAL-RAY ANGLE COEFFICIENTS

Isovelocity/Real-Ray Angle Coefficients						
Profile	Depth (Feet)	^a 0	^a 1	a ₂	Standard Deviation	θ _{MIN.} * Degrees
Standard 50 Foot Layer	6400 9600 12,800 16,000 25,600	8.6023 9.1153 8.2957 5.0734 -4.1881	0:6603 0.6226 0.6442 0.8200 1.2230	0.004213 0.004580 0.004413 0.001993 -0.002824	±0.2688 ±0.3446 ±0.3275 ±0.0762 ±0.2205	2 2 2 6 16
Standard 100 Foot Layer	6400 9600 12,800 16,000 25,600	8.5830 8.8283 8.0539 4.7018 -5.3533	0.6575 0.6394 0.6602 0.8417 1.2846	0.004051 0.004197 0.004199 0.001642 -0.003624	±0.3257 ±0.3230 ±0.3004 ±0.0735 ±0.3230	2 2 2 6 16
Standard 150 Foot Layer	6400 9600 12,800 16,000 25,600	8.2015 8.5083 7.7826 4.3802 -6.0692	0.6800 0.6594 0.6703 0.8616 1.3195	0.003792 0.004059 0.004105 0.001356 -0.004083	±0.3237 ±0.2962 ±0.2863 ±0.2035 ±0.3894	2 2 2 6 16
Standard 200 Foot Layer	6400 9600 12,800 16,000 25,600	7.8392 8.0729 7.1932 4.2367 -3.8743	0.7091 0.6832 0.7087 0.8610 1.1904	0.003424 0.003897 0.003510 0.001355 -0.002265	±0.2613 ±0.2645 ±0.2254 ±0.0644 ±0.1200	4 4 4 8 18
Standard 300 Foot Layer	6400 9600 12,800 16,000 25,600	7.4898 7.6342 6.6991 3.8759 -4.3241	0.7121 0.6993 0.7257 0.8760 1.2033	0.003468 0.003571 0.003225 0.001217 -0.002387	±0.2399 ±0.2460 ±0.2212 ±0.1382 ±0.1158	4 4 4 8 18
Standard 400 Foot Layer	6400 9600 12,800 16,000 25,600	. 6.7703 7.2025 6.1839 2.7324 -4.5184	0.7554 0.7099 0.7527 0.9477 1.2034	0.002769 0.003458 0.003021 0.000233 -0.002303	±0.2747 ±0.2188 ±0.2020 ±0.3097 ±0.1215	4 4 4 8 18
Temperate Summer 90 Foot Layer	6400 9600 12,800 16,000 25,600	10.8105 10.6152 9.6249 6.7419 -4.4007	0.5667 0.5615 0.5991 0.7527 1.2526	0.005255 0.005308 0.004836 0.002707 -0.003285	±0.3742 ±0.3730 ±0.3917 ±0.1513 ±0.2847	2 2 2 4 16
Temperate Autumn 260 Foot Layer	6400 9600 12,800 16,000 25,600	8.4710 8.1893 6.7723 3.6068 -5.4342	0.6676 0.6692 0.7266 0.8883 1.2542	0.004021 0.003965 0.003110 0.001142 -0.003012	±0.2818 ±0.2718 ±0.2283 ±0.0593 ±0.1717	* 4 4 4 8 18

TABLE 1. ISOVELOCITY/REAL-RAY ANGLE COEFFIC LENTS (Continued)

	ADLE I. I.			y Angle Coeffici		.4\
Profile	Depth (Feet)	a ₀	a 1	a 2	Standard Deviation	θ _{MIN} * (Degrees)
Temperate Winter 350 Foot Layer	6400 9600 12,800 16,000 25,600	3.8082 4.4706 1.0820 0.5318 -9.3678	0.8795 0.8296 0.8876 1.0083 1.4144	0.001232 0.001974 0.002349 -0.002682 -0.004823	±0.1780 ±0.1486 ±0.5132 ±0.1479 ±0.4047	4 4 8 10 18
Equator Summer 215 Foot Layer	6400 9600 12,800 16,000 25,600	10.1425 10.1572 9.0422 6.6005 -3.4573	0.6102 0.5962 0.6379 0.7588 1.2037	0.004671 0.004847 0.004252 0.002645 -0.002655	±0.2882 ±0.3291 ±0.3152 ±0.1591 ±0.2279	2 2 2 4 16
Equator Autumn 215 Foot Layer	6400 9600 12,800 16,000 25,600	9.5204 9.6214 8.7852 6.7517 -2.9756	0.6509 0.6333 0.6591 0.7503 1.1783	0.003782 0.004030 0.004052 0.002748 -0.002332	±0.2656 ±0.2537 ±0.2521 ±0.1578 ±0.1924	4 4 4 4 16
Equator Winter • 246 Foot Layer	6400 9600 12,800 16,000 25,600	9.4627 9.7181 8.9231 6.6245 -3.8493	0.6479 0.6155 0.6462 0.7504 1.2231	0.004053 0.004542 0.004080 0.002805 -0.002927	±0.2129 ±0.2463 ±0.3182 ±0.1439 ±0.2506	2 2 3 4 16
Polar Summer Zero Layer	6400 9600 12,800 16,000 25,600	-9.6344 -13.6549 -18.4531 -21.4276 -21.9089	1.4214 1.5721 1.7780 1.8700 1.9727	-0.004949 -0.006375 -0.008931 -0.009692 -0.009836	±0.2494 ±0.4530 ±0.5219 ±0.4870 ±0.1871	14 16 18 20 26
Polar Autumn Zero Layer	6400 9600 12,800 16,000 25 600	3.3871 -0.3767 -3.6426 -6.7215 -13.3254	0.8592 1.0361 1.1756 1.2971 1.4774	0.001752 -0.0004649 -0.002106 -0.003489 -0.004728	±0.1417 ±0.1561 ±0.1475 ±0.2888 ±0.1279	4 10 14 16 24
Polar Winter 462 Foot Layer	6400 9600 12,800 16,000 25,600	-1.9621 -4.1731 7.4945. -10.7718 -18.8003	1.0925 1.1687 1.3072 1.4317 1.6906	-0.009983 -0.001777 -0.003417 -0.004738 -0.007045	±0.1815 ±0.1272 ±0.2077 ±0.2356 ±0.1744	10 14 16 18 24

^{*} θ_{MIN} is the minimum ray angle that will strike the bottom. Angles less than θ_{MIN} are refracted upward before striking the bottom and do not give rise to bottom bounce eoverage. For ray angles greater than 50 degrees, the isoveloeity and real-ray angles can be assumed equal.

TABLE 2. BOTTOM BOUNCE CONSTANTS

Bottom Bounce Constant C'						
		Bot	tom Depth (Fo	om Depth (Fcet)		
Profile '	6400	9600	12,800	16,000	25,600	
STANDARD					١	
50 Foot Layer	0.97504	0.98297	0.99346	1.00436	1.03882	
100 Foot Layer	0.97562	0.98355	0.99405	1.00495	1.03944	
150 Foot Layer	0.97620	0.98414	0.99465	1.00555	1.04006	
200 Foot Layer	0.97679	0.98472	0.99524	1.00615	1.04067	
300 Foot Layer	0.97795	0.98590	0.99642	1.00735	1.04191	
400 Foot Layer	0.97912	0.98707	0.99761	1.00855	1.04316	
EQUATOR						
Autumn	0.97232	0.98082	0.99011	1.00099	1.03697	
Summer	0.97232	0.98102	0.99071	1.00118	1.03718	
Winter	0.97269	0.98100	0.99070	1.00119	1.03800	
TEMPERATE		٠				
Autumn	0.97790	0.98765	0.99701	1.00796	1.04940	
Summer	0.97268	0.98099	0.98931	1.00218	1.03841	
Winter	0.98438	0.99259	1.00280	1.01422	1.05026	
POLAR						
Autumn	1.00103	1.01301	1.02478	1.03613	1.07062	
Summer	1.02734	1.03963	1.05128	1.06336	1.09875	
Winter	1.01104	1.02250	1.03417	1.04563	1.08043	

(a) Mud Bottom

$$L_{B} = 0$$
 $\theta_{TB} \le 1$ $\theta_{TB} = 1.1 \; \theta_{TB} = 0.403$ $\theta_{TB} \ge 19$ $\theta_{TB} \ge 19$ $\theta_{TB} \ge 19$

(b) Mud/Sand Bottom

$$L_{B} = 0.1$$
 $\theta_{TB} \le 3$
 $L_{B} = .825 \, \theta_{TB} - 2.2549$ $3 < \theta_{TB} \le 25$
 $L_{B} = 17.4$ $\theta_{TB} > 25$

(c) Sand Bottom

$$L_{B} = 0$$
 $\theta_{TB} \le 5$
 $L_{B} = .365 \, \theta_{TB} - 1.738$ $5 < \theta_{TB} \le 36$
 $L_{B} = 11.5$ $\theta_{TB} > 36$

(d) Rock Bottom

$$L_{B} = 0$$
 $\theta_{TB} \le 21$ $\theta_{TB} \le 21$ $\theta_{TB} = 0$ $\theta_{TB} \le 21$ $\theta_{TB} \le 50$ $\theta_{TB} > 0$ $\theta_{TB} > 0$

The convergence zone mode of operation of the AN/SQS-26 is used to provide extremely long range detection capability by taking advantage of the refractive properties of the deep ocean. To determine the convergency zone range window and propagation losses within the window, acoustic ray path and propagation loss calculations were performed and provided by the USNUSL (Navy Underwater Sound Laboratory), (references 5 and 6). This data has been compiled in look-up tables and is not included in this report due to its voluminous content.

1.3 DEVICE 14844 PROPAGATION LOSS MODELS

This section provides the propagation loss models for the P-3C DIFAR Operator Trainer, Device 14B44 (reference 7). The math model for total propagation loss is given by the following equation:

$$TL_T = TL_1 + TL_2 + TL_3 - TG$$

where TLT = Total propagation loss

TL₁ = Loss due to spreading and attenuation

 TL_2 = Surface bounce loss

 TL_3 = Bottom bounce loss

TG = Convergence zone gain

The propagation loss is determined by linear approximations of transmission loss curves as shown in figure 2.

In the surface bounce mode of propagation, the propagation loss is determined as a function of sea state as indicated in table 3. The values in the table were determined by extrapolating Schulkins empirical curve (reference 8) which establishes the leakage loss as a function of frequency - waveheight product.

When operating in the bottom bounce mode of propagation, the loss due to reflection from the bottom is a function of bottom type only. In determining the bottom loss for simulation, average reflection values were taken for each of the three bottom types simulated. (References 9 and 10.) The bottom bounce loss is assumed to be zero for a hard bottom. For a medium and soft bottom the loss is assumed to be 3 dB and 9 dB respectively, as shown in table 4:

If a convergence zone exists between the source and receiver, a gain factor is subtracted from the total transmission loss. The convergence zone gain provides a minimum gain of 12 db with a further increase up to 3 db for the first convergence zone and up to 1.5 db for the second and third convergence zones as a function of the distance of the hydrophone to the center of the zone. The following model is based on a quantitative discussion of convergence zones by R. J. Urick (reference 9).

TG = 12 +
$$\frac{3}{N}$$
 $\frac{(1 - X_T - X_D)}{X_A}$

where X_T = Target to sonobuoy flat range

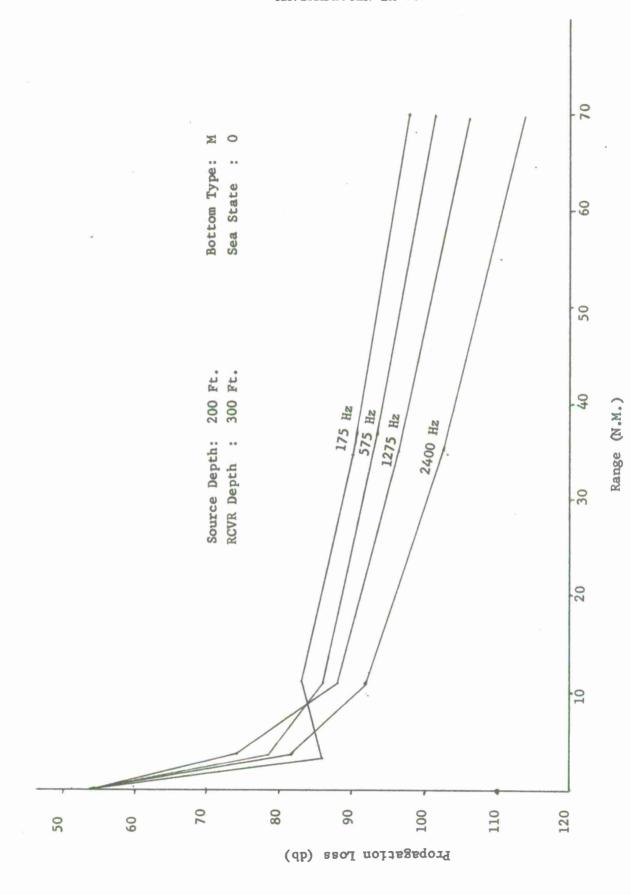


Figure 2. Propagation Loss Device 14844

TABLE 3. SURFACE BOUNCE LOSS

SURFACE BOUNCE	LOSS AS A FUNCTION OF SEA STATE
Sea State	Surface Bounce Loss (TL ₂)
0	2 db
1	2 db
2	3 db
3	4 db
4	6 db

TABLE 4. BOTTOM BOUNCE LOSS

BOTTOM BOUNCE LOSS AS	A FUNCTION OF BOTTOM TYPE
Bottom Type Bot	ttom Bounce Loss (TL ₃)
Hard	0 db
Medium	3 db
Soft	9 db

 X_D = Ranges between midpoint of convergence zone and target

 $X_A = 1/2$ convergence zone width

N = Number of the convergence zone

It is important to note that these models are limited to frequencies less than approximately 2500 Hz.

1.4 DEVICE 2F69, PROPAGATION LOSS MODELS

The objective of this section is to present the propagation loss math model for Device 2F69, P-3A Weapon System Trainer (reference 11). The sound energy is attenuated in the simulated environment by the following equation:

$$N = 20 \log R + (.2f + .00015 f^2) R + 60 db$$

where N = nominal statistical average propagation loss between two points (db) $\,$

where R = range from source (Kyd)

where f = signal frequency (kHz)

The frequency dependent term is small for low frequencies and would indicate a 20 db loss per range decade or again, the spreading loss varies as a function of the inverse of \mathbb{R}^2 .

1.5 DEVICE 21A37, PROPAGATION LOSS MODELS

This section describes the acoustic propagation loss model for Device 21A37, Submarine Fleet Ballistic Missile Training Facility (reference 12). The earlier sonar math modes for Device 21A37 were constructed on the basis of ray and wave acoustic theory, using references 13 and 14, and additional data was obtained from reference 15. T. Einstein of USNUSL pointed out that this procedure was erroneous since project AMOS showed that classical sound theory applied only for short ranges and at high frequencies. Consequently, work in this area was discontinued and USL Research Report 491 (reference 16) was adopted as the basis for sonar simulation. Two separate cases are considered:

- a. Shallow target and shallow sonar
- b. Deep target or deep sonar.

For a particular set of parameters, bottom-path detection range and direct path detection range should be investigated and the greater of the two chosen. Curve α represents the bottom path detection curve; curve β the direct-path detection curve for case a; and curve γ , the direct-path detection curve for case b. The curves for layer depths, 0 ft. and 400 ft., were obtained directly from the corresponding curves in reference 16. The curves corresponding to other values of layer depth were obtained by graphically interpolating between 0 ft. and 400 ft., curves. The curve for 100 ft. layer depth is shown in figure 3. Each curve is individually analyzed and subsequently approximated by linear segments.

1.6- DEVICE 21A39/2 PROPAGATION LOSS MODELS

This section provides the propagation loss models for Device 21A39/2 Sonar Room Tactical Team Trainer (reference 17) Transmission effects of the direct path mode of propagation are simulated as a function of range, frequency, layer depth, target depth and own ship depth. The total direct path propagation loss is taken as the sum of a nominal loss and a layer depth correction factor. The nominal propagation loss is shown in figure 4, for representative ranges between 1 and 100 Kyds. The layer depth correction factor A is defined by the following equations:

$$A = (Z/L) R \qquad Z \leq 2.7 L$$

$$A = (2.7) R Z > 2.7 L$$

where Z = Average of own ship and target depth (ft)

L = Layer depth (ft) R = Target range (Kyds)

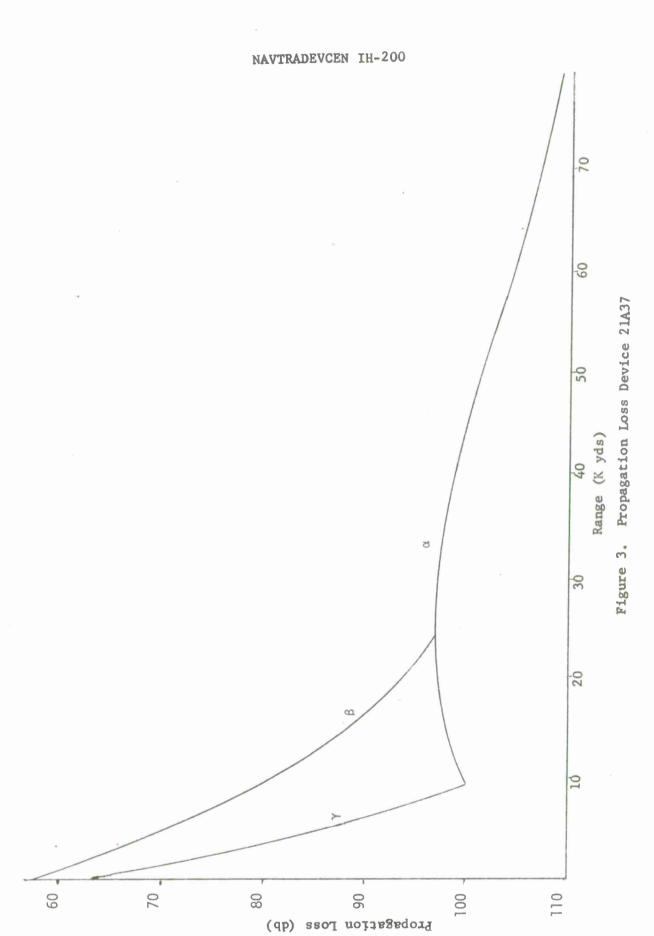
The minimum value of Z is 20 ft.

Transmission effects of the bottom bounce mode of propagation are simulated as a function of range and frequency as shown in figure 5. Bottom bounce loss equals the value at 4 Kyds for ranges less than 4 Kyds.

1.7 COMPARATIVE ANALYSIS AND MODEL SIMPLIFICATION

This section includes a discussion on the comparative analysis of the five previously discussed propagation loss math models and the NADC (Naval Air Development Center) ray trace model. The models have been analyzed on the basis of the major modes of propagation. Figures 6, 7, and 8 contain a comparative analysis of the direct path propagation, surface bounce propagation, and bottom bounce propagation respectively. The propagation loss curves were constructed from the various math models as a function of the variables listed in table 5. However, target and source depths, layer depth, temperature, sea state, bottom type and depth are not functions in all of the math models.

Analysis of the direct path propagation models, figure 6, shows that the propagation loss curves for Devices 21A39, 21A37, and 2F69 are approximately the same. Further analysis indicated that the propagation loss curve



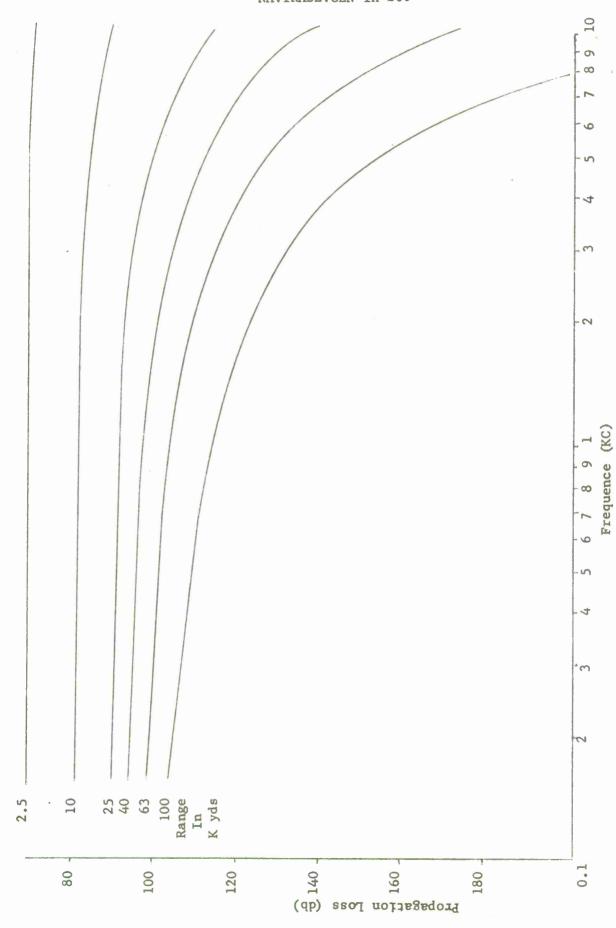


Figure 4. Nominal Direct Path Propagation Loss Device 21A39

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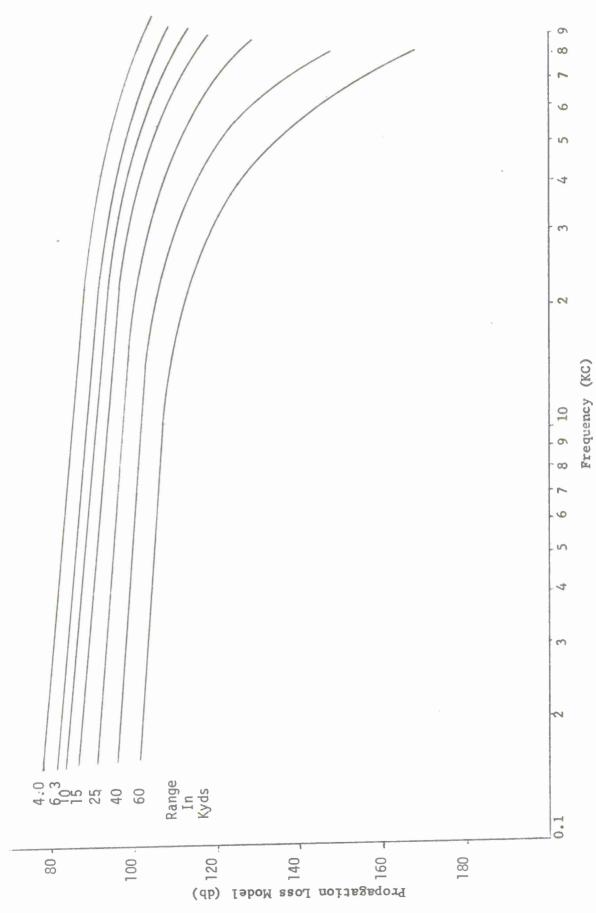
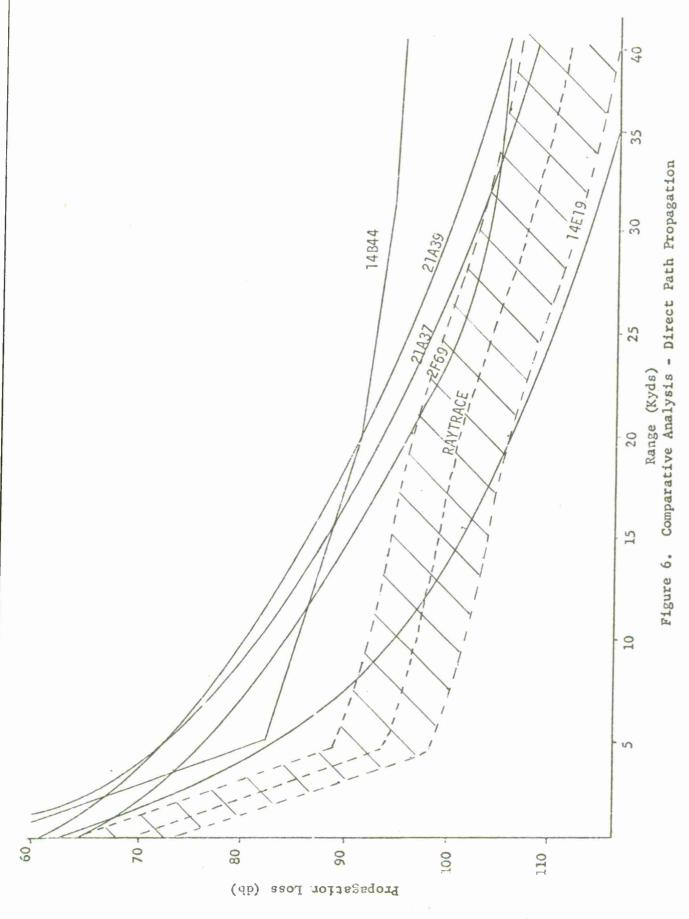
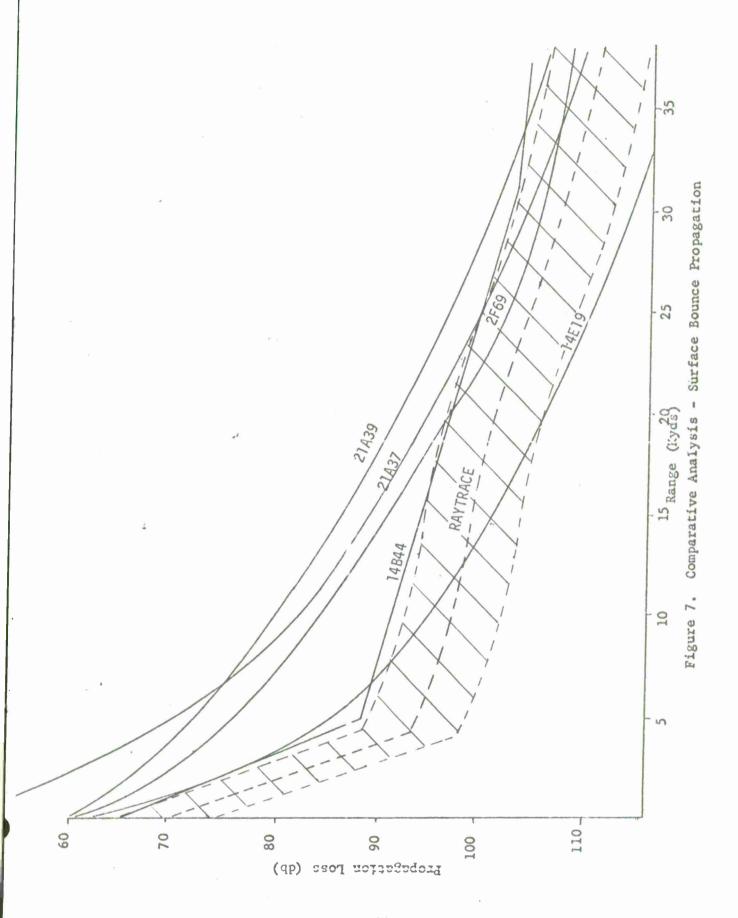


Figure 5. Bottom Bounce Propagation Loss Device 21A39





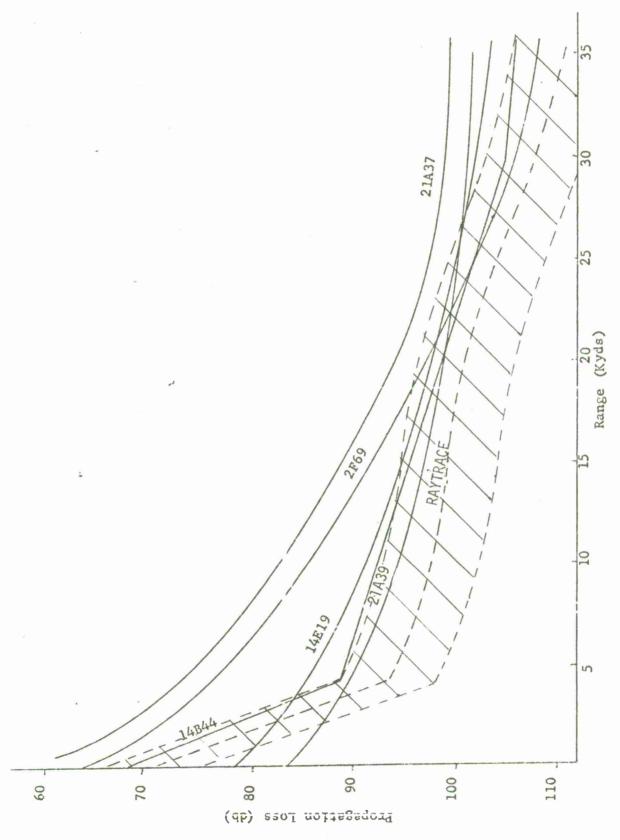


Figure 8. Comparative Analysis - Bottom Bounce Propagation

TABLE 5. MATH MODEL VARIABLES

Math Model Variables	Selected values
Target depth	200 feet
Source depth	20 feet
Layer depth	300 feet
Temperature	50° Fahrenheit
Sea state	<u>></u> 3
Bottom type	Soft
Bottom depth	12,800 feet
Range	0 - 35 Kyds
Frequency	2.5 kHz

for Device 14E19 consists of basically three separate slopes as a function of range. The slope for ranges less than 5 Kyds compares favorably with the other models discussed. The major problem arises from the slope of the curve for ranges between 5 and 25 kyds and the slope for ranges greater than 25 kyds. The goal to be realistically achieved would be ± 5 db of the NADC ray trace model. Therefore, tolerance limits have been set at ± 5 db and are shown by the shaded area.

Further analysis of figure 6 indicates definite break points in the propagation loss curve for Device 14B44. The propagation model consists of basically four parts: A basic loss term, a convergence zone term, a surface loss term, and a bottom loss term. The basic loss term is derived from Fleet Numericals' ASWEPS data package. ASWEPS is designed to function in all ocean areas. Incoming synoptic reports are summarized, analyzed, and then transmitted daily from the U.S. Naval Oceanographic Office. Passive sonar ranges are derived from a high speed propagation loss model valid for low frequencies. This model is a modified ray trace which calculates losses via surface duct, and convergence zones, assuming initially that the ocean is isovelocity and then making an empirical correction for refraction. The ASWEPS data is broken down for various ocean areas, summer and winter conditions, and a combination of four source and receiver depths. This information is provided at four discrete frequencies up to 1,700 Hz. The NADC ray trace model was chosen for comparison here since it is very similar to the ray trace model utilized in generating the ASWEPS curves.

In the Device 14B44 propagation loss model, all source and receiver depths have been averaged, then the data is averaged over winter and summer and finally averaged over all areas. The result is four curves, one for each frequency, of propagation loss versus range. These curves are then approximated with four linear approximations resulting in the definite break points in the curves. There are also very significant differences in propagation loss between different areas and also in the same area for different seasons which have an important bearing on training, as illustrated by the difference in the propagation loss resulting from the averaging of depths, seasons, and latitudes in the Device 14B44 model.

Analysis of the surface bounce propagation models, figure 7, again shows the steeper slope of the Device 14E19 propagation loss curve and the definite break points in the Device 14B44 propagation loss curve. Although the basic loss term for the Device 14B44 propagation loss model is derived from the ASWEPS data, the surface loss term is derived from AMOS data. The data from which the AMOS results were derived only covered the frequency range from 2 KHz to 25 KHz. The AMOS results were not intended to be used at low frequencies. To extend these results below 2 KHz will

result in error. An error exists in the fact that the same surface bounce loss is added to the basic curves at all ranges. In the real world the surface bounce loss increases as a function of range and the number of surface bounces. Still another error exists in that the surface loss has previously been included in the composite ASWEPS data and should not be included a second time.

Analysis of the bottom bounce propagation models, figure 8, reveals an unusually large initial propagation loss variation. The deviation here can-be as much as 25 dB and should be revised by adding a correction factor for short ranges.

The bottom bounce propagation loss model for Device 14E19 was based on the assumption of ideal straight line (isovelocity) propagation paths. In the real world, the ocean rarely provides ideal isovelocity conditions and the propagation paths differ radically from straight line paths. The variation depends on the ocean velocity structure. Even though real ray angles are computed from the equivalent isovelocity angles, it appears as though an error is introduced here, particularly at short ranges.

In the Device 14B44 bottom bounce propagation model, if the bottom loss is considered important, a loss of 0, 3, or 9 dB is added to the basic loss term depending on the bottom type. The same bottom loss is added to the basic curves at all ranges. This is contrary to what actually happens. Operating in deep water at low frequencies, energy incident on the bottom at low grazing angles suffers considerably less than higher grazing angles. The same error also arises here as in the surface loss propagation model, in that the bottom loss has previously been included in the composite ASWEPS data and should not be included a second time.

To aid in error analysis, relative error was plotted versus range for each model and each major mode of propagation as shown in figures 9, 10, and 11. A positive error indicates a decreased propagation loss resulting in a stronger signal strength and premature target detection. A negative error indicates too great a magnitude of propagation loss resulting in a weaker signal and delayed target detection. At short ranges it is shown that the error is consistantly positive, resulting in premature target detection. At greater ranges, it is found that the relative error is still generally positive although considerably less than that found at shorter ranges.

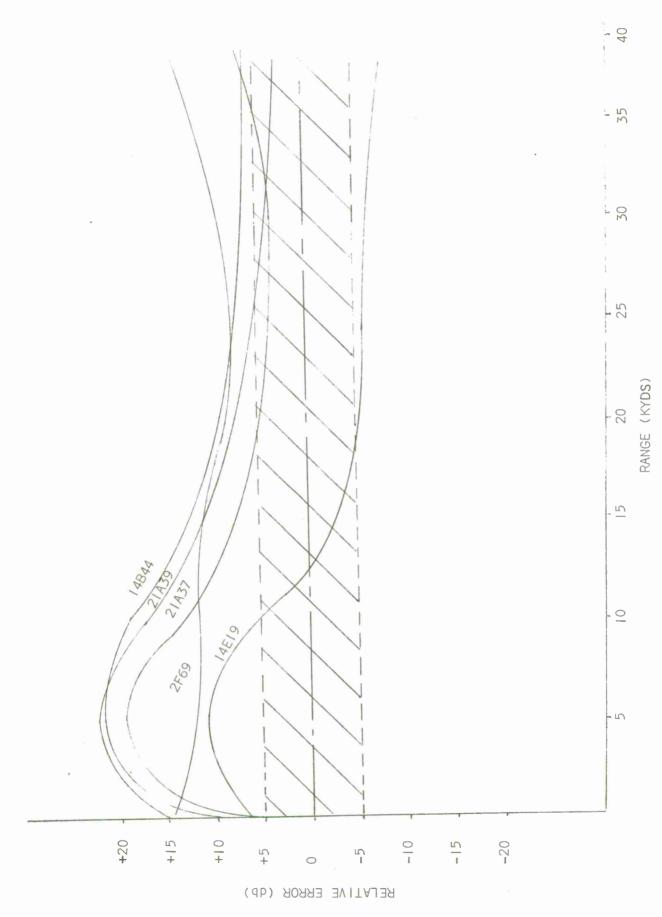


Figure 9. Relative Error -- Direct Path Propagation

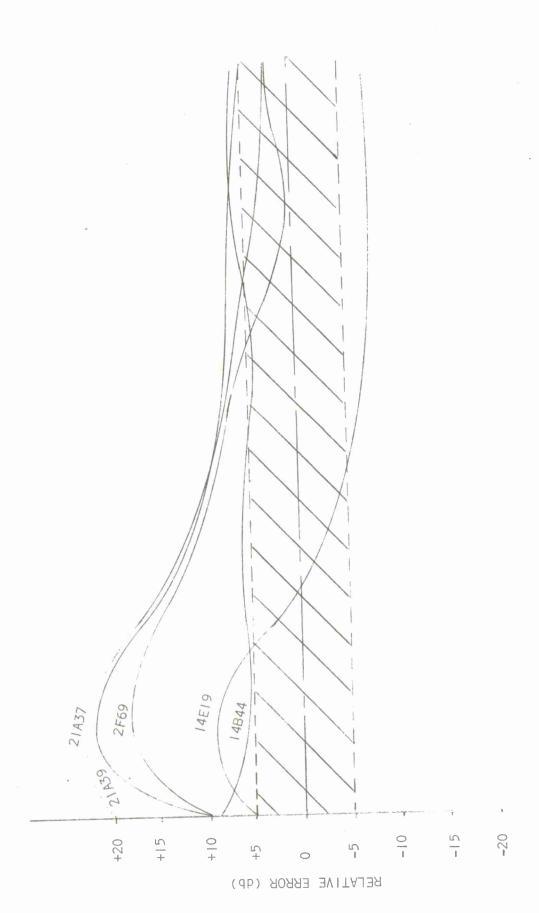




Figure 10. Relative Error -- Surface Bounce Propagation

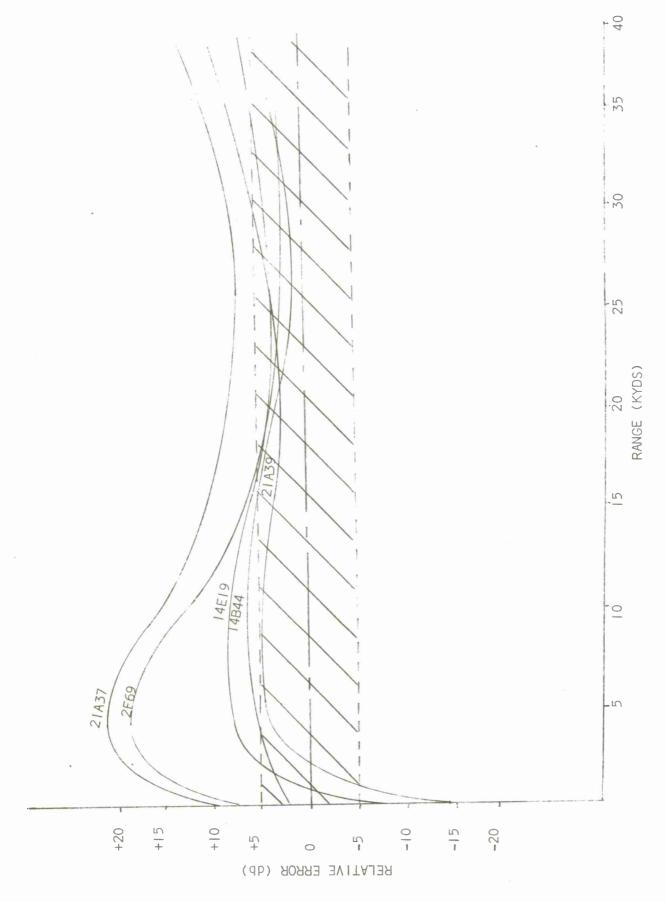


Figure II. Relative Error -- Bottom Bounce Propagation

LIST OF REFERENCES

- 1. Final Math Model Report for Basic Operator/Team Trainer for the AN/SQS-26-CX Sonar, Device 14E19, Honeywell Report, March 1971
- 2. MARSH, H. W. and SCHULKIN, M. "Report on the Status of Project AMOS," Navy Underwater Sound Laboratory Report No. 255A, 9 May 1967
- 3. DAVIDSON, R. O., et. al., "Propagation Loss Routines for an ASW Simulation Program," Vitro Report VL-2471-1-9, 10 April 1967
- 4. "Proposed Operating Doctrine for the AN/SQS 26AXR/CX; Trainees Guide for Sonar Technician Training," AN/SQS-26 Operation Staff Fleet Sonar School, Keywest, Oct. 1969
- 5. WEINBERG, H. "CONGRATS I: Ray Plotting and Eizenray Generation," Navy Underwater Sound Laboratory, Report No. 1052, 30 Oct. 1969
- 6. COHEN, J.S. and EINSTEIN, L.T. "CONGRATS II: Eizenray Processing Programs," Navy Underwater Sound Laboratory Report No. 1069, 5 Feb. 1970
- 7. Ocean Environment Simulation Criteria Report for 14B44 P-3C DIFAR Operator Trainer, Singer-General Precision, Inc. Report No. 8266-114, June 1970
- 8. USL Report No. 1013; "The Propagation of Sound in Imperfect Ocean Surface Ducts"; SCHULKIN, M. USN Underwater Sound Lab; Fort Trunbull, New London, Connecticut; 1969
- 9. URICK, R. J. "Principles of Underwater Sound for Engineers" New York, N. Y.; McGraw-Hill, 1967
- 10. SP-84 "Oceanography and Underwater Sound for Naval Application", Oceanographic Analysis Division, Marine Sciences Department, Washington, D.C.
- 11. Final Engineering Design Report for Underwater Sound Design Criteria of Device 2F69B, General Precision, Inc., Report No. 8134-120, Feb. 1967
- 12. Math Model Report for Submarine Fleet Ballistic Missile Training Facility, Honeywell Report, 31 Dec. 1963
- 13. HORTON, J.W., "Fundamentals of Sonar," United States Naval Institute, Anapolis, Maryland, 1959

- 14. U.S. Office of Scientific Research, "Physics of Sound in the Sea," Summary of Technical Report of Division 6 NRDC, VI 8, Washington, 1946
- 15. Woods Hole Oceanographic Institute, "Sound Beam Patterns in Sea Water," Oct. 10, 1944
- 16. BELL, Thaddeus, "Sonar Detection and Detectability Range for Submarines," Navy Underwater Sound Lab., USL Research Dept. #491, 21 Oct. 1960, CONFIDENTIAL
- 17. Sonar Room Operator Trainer, Device 21A39/2, NAVTRADEVCEN Specification.

APPENDIX A

SYMBOL DEFINITIONS

L = Surface isothermal layer depth

S = Sea state

T = Water Temperature

R_H = Horizontal Range

 $R_s = Slant Range$

Z = Ownship depth

z = Target depth

f = Acoustic frequency

 N_W = Transmission loss

a = Absorption coefficient

as = Scattering coefficient

G = First depth loss factor

H = Second depth loss factor

 $r, r_1, z, z_0 = Scaled variables$

 θ_{Bi} = Isovelocity range angle

θ_{TBi} = Transmitted deviation loss angle

 θ_{TB} = Real bottom grazing angle

 D_{Bi} = Depth of bottom

 D_T = Depth of target

 L_B = Bottom bounce loss as function of bottom type

 TL_T = Total propagation loss

TL1 = Loss due to spreading and attenuation

TL₂ = Surface bounce loss

APPENDIX A (Continued)

 TL_3 = Bottom bounce loss

TG = Convergence zone

 X_T = Target to sonobuoy flat range

 X_{D} = Range between midpoint of convergence zone and target

 $X_A = 1/2$ convergence zone width

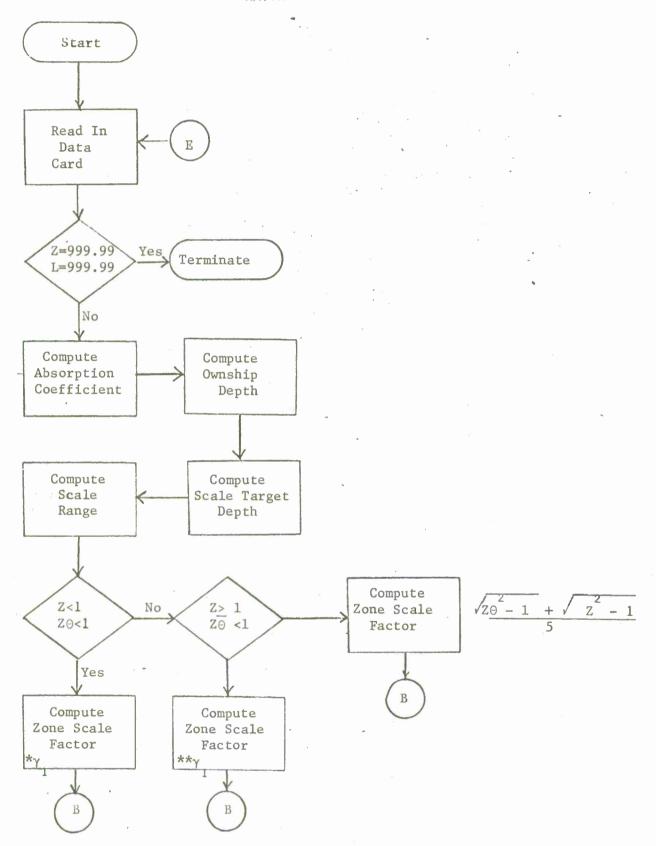
N = Number of convergence zone

A = Layer depth correction factor

APPENDIX B

FLOW DIAGRAM AND FORTRAN IV PROGRAM

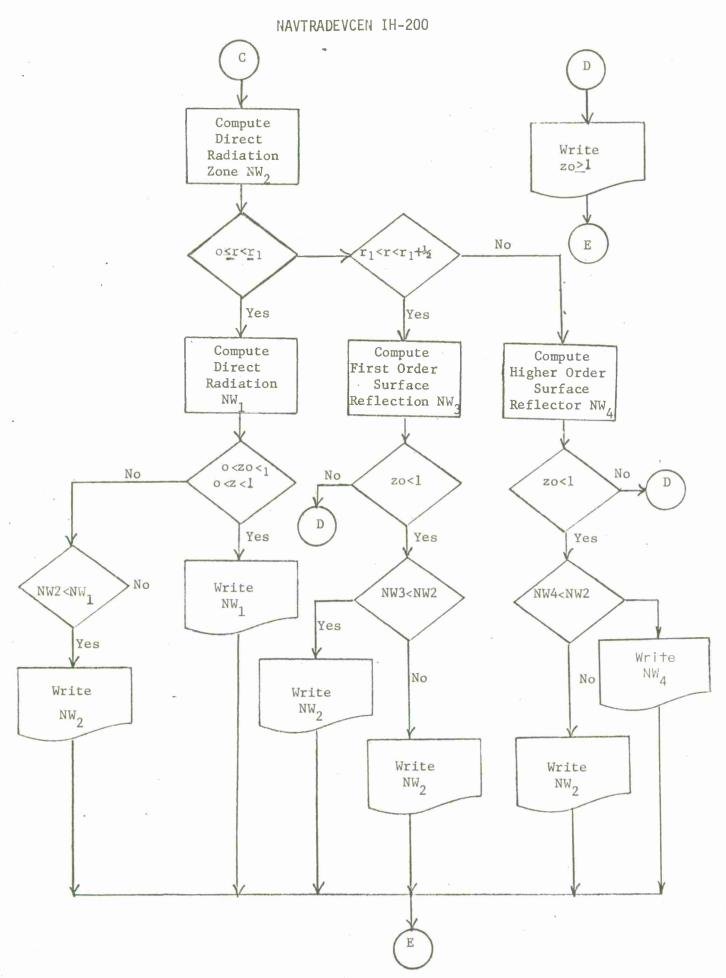
Appendix B contains the flow diagram and FORTRAN IV Program for Device 14E19 math model. The FORTRAN Program was generated by J. H. Gardner (Code 38) to aid in calculating the Device 14E19 math model from the following input data; target depth, layer depth, own ship depth, actual range, acoustic frequency, and sea state. With this program many sets of data can be computed on the Sigma 7 computer in a reasonably short time for comparative analysis with other math models.





Coefficient

Coefficient



CALCULATION OF PROPAGATION LOSS FOR DEVICE 14E19

J. H. GARDNER - CODE 381

```
SURFACE BOUNCE WITH SHADOW ZONE
DIRECT PATH WITH SHADOW ZONE
DATA INPUT AND VARIABLES WILL BE READ AS
           HORIZONTAL RANGE = HRANGE
               SLANT RANGE = SLANTR
       BIG Z = TARGET DEPTH = TDEPTH
        BIG L = LAYER DEPTH = XDEPTH
    BIG ZO = OWN SHIP DEPTH = ODEPTH
                  SEA STATE = JSEA
     F = ACOUSTIC FREQUENCY = ACFREQ
               BOTTOM SLOPE = BSLOPE
           DEPRESSION ANGLE = DEPRAG
               BOTTOM DEPTH = BDEPTH
               SCALED RANGE = SRANGE
     ABSORPTION COEFFICIENT = A
               ACTUAL RANGE = ARANGE
       SCALED OWNSHIP DEPTH = ZO
        SCALED TARGET DEPTH = Z
   SHADOW ZONE SCALE FACTOR = SZSF
```

```
FIRST DEPTH - LOSS FACTOR(DB) = G
       SECONDDEPTH - LOSS FACTOR(DB) = H
       FORMAT (4F6.2, F7.2,11)
7
       READ (105, 5) TDEPTH, XDEPTH, ODEPTH, ARANGE, ACFREQ, JSEA
       IF (TDEPTH .EO. 999.99) IF (XDEPTH .EO. 999.99)
      $STOP
       COMPUTE ABSORPTION COEFFICIENT***COMPUTE SCALE OWNSHIP DEPTH
       COMPUTE SCALE TARGET DEPTH***COMPUTE SCALE RANGE
       A = 0.033*ACFREQ **(3./2)
              = (ODEPTH/XDEPTH)**.5
       Z0
              = (TDEPTH/XDEPTH)**.5
       SRANGE = ARANGE/(XDEPTH)**.5
       IF (Z<1.) IF (ZO<1.) SZSF=((1.-ZO)/4.)+(SQRT((Z**2.)-1))/5.);
       GO TO 3
       SZSF = (SORT((Z0**2.) - 1.) + SORT((Z**2.)-1.))/5.
       COMPUTE FIRST DEPTH - LOSS FACTOR
       IF (Z - ZO < 1.) GO TO 8
3
       G = ((ACFREO/25.)**(1./3.))*20.
       GO TO 9
       G = ((.1)*(10.)**(2.3*(Z - Z0)))*((ACFREO/25.)**.3334)
```

```
9 IF (ACFREO < 8.) GO TO 10
   COMPUTE SECOND DEPTH LOSS FACTOR
   H = .4*((ACFREQ/8.)**(1./3.))*((10.**(Z-ZO)) + (10.**Z) + (10.**ZO))
    GO TO 11
10 H = .4*((10.**(Z-Z0))+(10.**Z)+(10.**Z0))
11 IF (JSEA < 3) GO TO 12
    COMPUTE SCATTERING ATTENUATION COEFFICIENT
    AS = ((ACFREQ/XDEPTH)**.5)*9.
    GO TO 14
12 AS = ((ACFREQ/XDEPTH)**.5)*4.5
    BASIC AMOS PROPAGATION LOSS***START WITH XNW2
14 XYZ = 25.-((ABS(TDEPTH-XDEPTH))**.5) - ((ABS(ODEPTH-XDEPTH))**.5)
    1+5. * ARANGE
    IF (XYZ)15,16,16
   XYZ = 0.0
15
   XNW2 = 20. * (ALOG10(ARANGE)) + (A * ARANGE) + XYZ * ((ACFREQ/25.))
    1**(1./3.)) + 60.
    COMPUTE DIRECT RADIATION ZONE
    IF (SRANGE .GE. 0.)IF(SRANGE < SZSF) GO TO 20</pre>
    IF(SZSF < SRANGE) IF (SRANGE < SZSF +.5) GO TO 21
    IF (SZSF + .5 < SRANGE) GO TO 22
20 XNW1=20.*ALOG10(ARANGE)+(A*ARANGE)+(G*(SRANGE/SZSF)+60.)
    IF (Z0 > 0.) IF (Z > 0.) IF (Z0 < 1.) IF (Z < 1.)
   $WRITE (108.30)XNW1; GO TO 7
    IF (XNW2 > XNW1)WRITE (108,30)XNW1; GO TO 7
    WRITE (108,31) XNW2
    GO TO 7
21 XNW3 = 20.*(ALOG10(ARANGE)) + (A*ARANGE) + 2.*(SRANGE-SZSF)*H+
   (1.-2.*(SRANGE - SZSF))* G + 60.
    IF (ZO > 1.) WRITE (108,36); GO TO 7
    IF XNW2 > XNW3)WRITE(108,32)XNW3; GO TO 7
    WRITE (108,33)XNW2
    GO TO 7
22 XNW4 - 10. * (ALOG10(ARANGE))+(A+AS)* ARANGE + H
    1-AS * ((XDEPTH **.5) * (SZSF + .5)) + 10. *
    2(ALOG 10((XDEPTH ** .5) * (SZSF + .5))) + 60.
    IF (ZO > 1.) WRITE (108,37); GO TO 7
    IF (XNW2 > XNW4) WRITE (108,34)XNW4; GO TO 7
    WRITE (108,35) XNW2
    GO TO 7
30 FORMAT (3/30H WITHIN DIRECT RADIATION ZONE \frac{1}{12},8HNW(1) = \frac{1}{12},6.2,
   $4H(DB))
   FORMAT (3/30H WITHIN DIRECT RADIATION ZONE, //12X, 8HNW(2) = ,F6.2,
   $4H(DB))
   FORMAT (3/62H WITHIN ZONE OF FIRST ORDER SURFACE REFLECTION AND SHA
   $DOW ZONE//12X,8HNW(3) = ,F6.2,4H(DB))
   FORMAT (3/62H WITHIN ZONE OF FIRST ORDER SURFACE REFLECTION AND SHA
   DOW ZONE//12X,8HNW(2) = F6.2,4H(DB)
   FORMAT (3/ 'WITHIN ZONE OF SECOND OR HIGHER ORDER SURFACE REFLECT
   10N ZONE'/12X,8HNW(4) = ,F6.2,4H(DB)
```

- 35 FORMAT (3/ 'WITHIN ZONE OF SECOND OR HIGHER ORDER SURFACE REFLECT
 \$10N ZONE'/12X,8HNW(2) = ,F6.2,4H(DB))
 36 FORMAT (3/ 'ZO> 1,WITHIN ZONE OF FIRST ORDER SURFACE REFLECTOR AND
 1 SHADOW ZONE--NW3')
- 37 FORMAT (3/ 'ZO > 1, WITHIN ZONE OF SECOND OR HIGHER ORDER SURFACE R 1EFLECTION ZONE--NW4') END